

# Ferroelectric Film Dynamics Simulated by a Second-order Time-dependent Landau Model

Michael S. Richman<sup>1</sup>\*, Paul Rulis<sup>1</sup>, and Anthony N. Caruso<sup>1</sup>

<sup>1</sup>Department of Physics and Astronomy, University of Missouri-Kansas City  
5110 Rockhill Road, Kansas City, Missouri, 64110

\*Michael S. Richman: msrxt4@mail.umkc.edu

Based on the work of B. Wang *et al.* [J. Appl. Phys., **94**, 3384 (2003)] that established a second-order time-dependent Ginzburg–Landau equation and a model for domain switching in ferroelectric films that employs this equation, we simulate the reaction of a ferroelectric film system’s polarization  $\tilde{P}$  to an applied electric field  $\tilde{E} = \tilde{E}_0 \sin(\tilde{\omega}\tilde{t})$  where  $\tilde{E}_0$ ,  $\tilde{\omega}$ , and  $\tilde{t}$  represent field amplitude, field frequency, and time, respectively. Polarization hysteresis loop structure as a function of  $\tilde{E}_0$  and  $\tilde{\omega}$  are examined. The relationship between hysteresis loop area  $\langle \tilde{A} \rangle$  and  $\tilde{\omega}$ , i.e., hysteresis dispersion, is calculated.  $\langle \tilde{A} \rangle$  represents the energy dissipated during one cycle of the applied field. Departing from the work of Y.-L. Wang *et al.* [J. Mater. Sci., **46**, 2695 (2011)] that established the considered model produces experimentally expected hysteresis dispersion in the low- $\tilde{\omega}$  regime, we demonstrate that this model also produces experimentally expected hysteresis dispersion in the high- $\tilde{\omega}$  regime. Furthermore, we determine that this dispersion implies, in agreement with empirical observations, that a characteristic time  $\tau_1$  exists for system relaxation and that this time is inversely proportional to  $\tilde{E}_0$  when the latter is sufficiently high. It is the value of  $\tau_1$  relative to  $\tilde{\omega}^{-1}$  that determines whether or not complete domain reversal occurs. We also determine the dependence between field parameters and whether  $\tilde{P}$  exhibits a symmetry-restoring oscillation (SRO) or a symmetry-breaking oscillation (SBO). Only SROs exhibit a symmetry identical to that of the applied field, i.e.,  $X(\tilde{t}) = -X(\tilde{t} + T/2)$  where  $T$  represents the period of the applied field and  $X$  represents  $\tilde{E}$  or  $\tilde{P}$ .

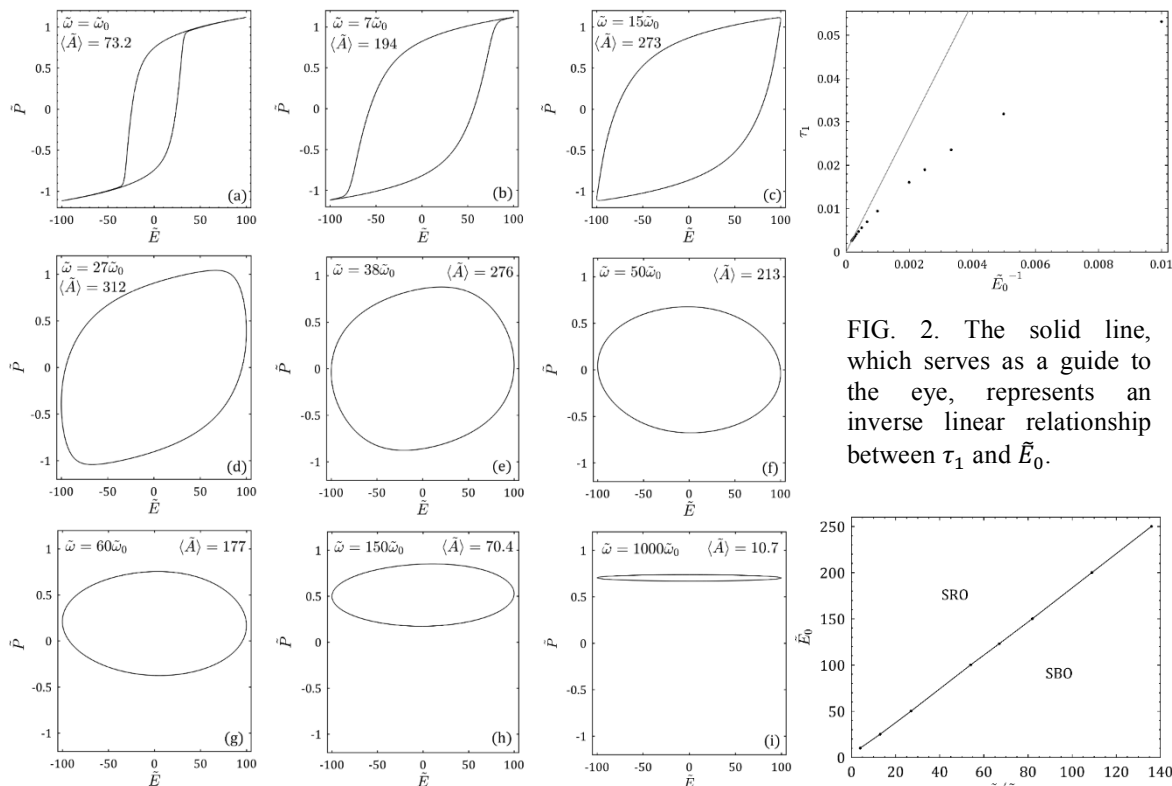


FIG. 1. Steady-state hysteresis loops for  $\tilde{E}_0 = 100$  and the field frequencies indicated. The area  $\langle \tilde{A} \rangle$  of each loop is displayed.

FIG. 2. The solid line, which serves as a guide to the eye, represents an inverse linear relationship between  $\tau_1$  and  $\tilde{E}_0$ .

FIG. 3. Bifurcation curve indicating whether a SRO or a SBO exists for the parameters indicated.